Lecture 11: Introduction to NumPy

Morten Rieger Hannemose, Vedrana Andersen Dahl Fall 2023



Num Py Operations

Today's lecture

- 1. Introduction to NumPy (ca. 5 min)
- 2. NumPy Arrays and Operations (ca. 30 min)
- 3. Previous exam question (ca. 15 min)

Num Py Operations

Motivation

- Lists can contain numbers, and we can perform any computation on them we desire.
 - Is this not enough?

Example: Adding Lists

```
1 list1 = [1, 2, 3]
2 list2 = [4, 5, 6]
3 result = []
4 for i in range(len(list1)):
5 result.append(list1[i] + list2[i])
```



Motivation

- Lists can contain numbers, and we can perform any computation on them we desire.
 - Is this not enough?
- For numerical data in arrays, lists are slower and less practical.
- NumPy provides
 - n-dimensional arrays
 - tools to work with these arrays.
- NumPy allows vectorized operations for efficient array calculations.
- Operations can be performed element-wise without explicit looping.

Example: Adding Lists

```
1 list1 = [1, 2, 3]
2 list2 = [4, 5, 6]
3 result = []
4 for i in range(len(list1)):
5 result.append(list1[i] + list2[i])
```

Example: Adding NumPy arrays

```
import numpy as np
arr1 = np.array([1, 2, 3])
arr2 = np.array([4, 5, 6])
result = arr1 + arr2
```

NumPy

import numpy as np

- A Widely used package in scientific computing, data analysis, and machine learning.
- ▶ It is the de facto standard for working with numerical data in Python.
- Several other libraries are built on top of NumPy, such as Pandas, SciPy, Scikit-learn, and Scikit-image.
- We use arrays to represent matrices and vectors.
- Don't call your files numpy.py

Num Py Arrays ●○○

NumPy Arrays: Multidimensional Arrays

Working with 2D Arrays

- NumPy supports multidimensional arrays.
- Accessing elements using indices, similar to lists.
- Reshaping:
 - The method .reshape().
 - The attribute . The shape is mutable.

Mutability of Arrays and Binary Indexing

- ▶ In NumPy, arrays are mutable, like lists.
- However, changes to a slice directly affect the original array.

```
Boolean Indexing and Mutability
```

```
i import numpy as np
2 arr = np.array([1, 2, 3, 4, 5])
3 # Create a boolean mask
4 mask = arr > 2
5 arr[mask] = 10
6 print(arr)
7 arr2 = arr[mask]
8 arr2[-1] = -5
9 print(arr)
```

```
Num Py Arrays
```

Num Py Operations

NumPy Arrays: Creation

- Lists are designed to be used with .append().
- ► For NumPy we should pre-allocate arrays
- Preallocation:
 - Don't iteratively grow the size of an array.
 - Create the array with the correct size before a for-loop.

```
Creating NumPy Arrays

i import numpy as np

a arr = np.array([1, 2, 3, 4, 5]) # array from lists (of lists etc.)

arr_zeros = np.zeros((3, 4)) # array with only 0

arr_ones = np.ones((2, 3)) # array with only 1

arr_range = np.arange(0, 10, 2) # like range
```

NumPy Operations: Universal Functions (ufuncs)

Universal Functions

```
1 arr = np.array([1, 2, 3])
2
3 sqrt_arr = np.sqrt(arr)
4 exp_arr = np.exp(arr)
5 sin_arr = np.sin(arr)
```

- Universal Functions (ufuncs) apply element-wise operations.
- For example:
 - np.sqrt()
 - np.exp()
 np.sin()

Num Py Operations

NumPy Operations: Broadcasting

Broadcasting

```
1 arr1 = np.array([[1, 2, 3], [4, 5, 6]])
2 arr2 = np.array([10, 20, 30])
3
4 result = arr1 + arr2
```

- Broadcasting enables operations on arrays of different shapes and sizes.
- NumPy handles shape mismatches.
 - We can add a 1D array to a 2D array.

Num Py Operations

Matrix Operations in NumPy

Matrix Operations

 NumPy provides syntax for linear algebra with matrices. Statistics

Statistics

```
1 data = np.array([1, 2, 3, 4, 5])
2 mean_value = data.mean()
3 std_dev = data.std()
4 median = np.median(data)
```

- NumPy provides functions for statistical calculations.
- axis keyword (e.g., .std(1)).

Final notes

- Some often used NumPy methods are accessible in multiple ways
 - x.mean() is the same as np.mean(x)
- ▶ The method will almost always exist on the np module.

- There is a class called numpy.matrix
- Don't use it!
- From NumPy's documentation:
 - "It is no longer recommended to use this class, even for linear algebra. Instead use regular arrays. The class may be removed in the future."

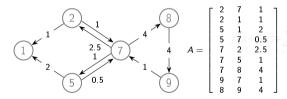
Num Py Operations

Coding example

node_divergence.py, exam from June 2021.

Node divergence

A graph can be represented using a 2D array where every row contains a triplet of numbers (i, j, w_{ij}) representing one graph edge. Here, *i* is an index of from-node, *j* is an index of to-node, and w_{ij} is the weight of the edge from *i* to *j*. For example, consider the graph in the illustration and its representation using *A*.



A = np.array([[2, 7, 1], [2, 1, 1], [5, 1, 2], [5, 7, 0.5], [7, 2, 2.5], [7, 5, 1], [7, 8, 4], [9, 7, 1], [8, 9, 4]]) The divergence of node *i* is defined as

$$d_i = \sum_{\substack{j \ \mathsf{edg\,e}{ij}}} w_{ij} - \sum_{\substack{j \ \mathsf{edg\,e}{ji}}} w_{ji}.$$

So d_i is the difference between the sum of weights of all edges originating from i and the sum of weights of all edges ending in i. For example

$$d_7 = (2.5 + 1 + 4) - (1 + 0.5 + 1) = 5$$

Problem definition

Create a function node_divergence that takes a 2D array representing a graph as input. The function should return an array containing sorted indices for graph nodes in one column and the divergence values for the corresponding nodes in the second column.

Node Divergence Solution

```
import numpy as np
def node_divergence(A):
    nodes = np.unique(A[:, :2])
    return_arr = np.zeros((nodes.shape[0], 2))
    return_arr[:, 0] = nodes
    for i in range(nodes.shape[0]):
        node = nodes[i]
        divergence = A[A[:, 0] == node, 2].sum() - A[A[:, 1] == node, 2].sum()
        return_arr[i, 1] = divergence
    return return_arr
```

もちゃく 御 そうやく 御 やく 白 やく