# Lecture 11: Introduction to NumPy 

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## Today's lecture

1. Introduction to NumPy (ca. 5 min )
2. NumPy Arrays and Operations (ca. 30 min )
3. Previous exam question (ca. 15 min )

- Lists can contain numbers, and we can perform any computation on them we desire.
$\nabla$ Is this not enough?


## Example: Adding Lists

```
list1 = [1, 2, 3]
list2 = [4, 5, 6]
result = []
for i in range(len(list1)):
    result.append(list1[i] + list2[i])
```


## Motivation

- Lists can contain numbers, and we can perform any computation on them we desire.
- Is this not enough?
- For numerical data in arrays, lists are slower and less practical.
- NumPy provides
- $n$-dimensional arrays
- tools to work with these arrays.
- NumPy allows vectorized operations for efficient array calculations.
- Operations can be performed element-wise without explicit looping.


## Example: Adding Lists

```
list1 = [1, 2, 3]
list2 = [4, 5, 6]
result = []
for i in range(len(list1)):
    result.append(list1[i] + list2[i])
```


## Example: Adding NumPy arrays

```
import numpy as np
arr1 = np.array([1, 2, 3])
arr2 = np.array([4, 5, 6])
result = arr1 + arr2
```


## NumPy

## import numpy as np

- A Widely used package in scientific computing, data analysis, and machine learning.
- It is the de facto standard for working with numerical data in Python.
- Several other libraries are built on top of NumPy, such as Pandas, SciPy, Scikit-learn, and Scikit-image.
- We use arrays to represent matrices and vectors.
- Don't call your files numpy.py


## NumPy Arrays: Multidimensional Arrays

```
Working with 2D Arrays
1 arr = np.array([1,2,3])
2 arr = np.array([[1, 2, 3], [4, 5, 6]]) # 2D array (2x3)
3 print("Arr has shape", arr.shape)
4 print(arr[0][1]) # looks like list, but inconvenient
5 print(arr[0, 1])
6 print(arr[:, 1])
7 # slicing
8 print(arr[:, 1:3])
```


## Mutability of Arrays and Binary Indexing

- In NumPy, arrays are mutable, like lists.
- However, changes to a slice directly affect the original array.

```
Boolean Indexing and Mutability
import numpy as np
arr = np.array([1, 2, 3, 4, 5])
# Create a boolean mask
mask = arr > 2
arr[mask] = 10
print(arr)
arr2 = arr[mask]
arr2[-1] = -5
print(arr)
```

NumPy Arrays: Creation

- Lists are designed to be used with .append().
- For NumPy we should pre-allocate arrays
- Preallocation:
- Don't iteratively grow the size of an array.
- Create the array with the correct size before a for-loop.

```
Creating NumPy Arrays
import numpy as np
arr = np.array([1, 2, 3, 4, 5]) # array from lists (of lists etc.)
arr_zeros = np.zeros((3, 4)) # array with only 0
arr_ones = np.ones((2, 3)) # array with only 1
arr_range = np.arange(0, 10, 2) # like range
```


## NumPy Operations: Universal Functions (ufuncs)

## Universal Functions

```
arr = np.array([1, 2, 3])
sqrt_arr = np.sqrt(arr)
exp_arr = np.exp(arr)
sin_arr = np.sin(arr)
```

- Universal Functions (ufuncs) apply element-wise operations.
- For example:
$>$ np.sqrt()
$\rightarrow n p \cdot \exp ()$
$\Rightarrow n p \cdot \sin ()$


## NumPy Operations: Broadcasting

```
Broadcasting
arr1 = np.array([[1, 2, 3], [4, 5, 6]])
2 arr2 = np.array([10, 20, 30])
4 result = arr1 + arr2
```

- Broadcasting enables operations on arrays of different shapes and sizes.
- NumPy handles shape mismatches.
- We can add a 1D array to a 2D array

Matrix Operations in NumPy

```
Matrix Operations
mat1 = np.array([[1, 2, 3],
    [3, 4, 5],
    [6, 7, 8]])
vec1 = np.array([5, 3, 2])
mat1 = np.array([[1, 2, 3],
    [3, 4, 5],
    [6, 7, 8]])
mat1.dot(vec1) # matrix-vector multiplication
mat1.dot(mat2) # matrix-matrix multiplication
mat1.T # matrix transpose
```

- NumPy provides syntax for linear algebra with matrices.


## Statistics

```
Statistics
data = np.array([1, 2, 3, 4, 5])
mean_value = data.mean()
std_dev = data.std()
median = np.median(data)
```


## Final notes

- Some often used NumPy methods are accessible in multiple ways
- x.mean() is the same as np.mean( x )
- The method will almost always exist on the np module.
- There is a class called numpy.matrix
- Don't use it!
- From NumPy's documentation:
- "It is no longer recommended to use this class, even for linear algebra. Instead use regular arrays. The class may be removed in the future."


## Coding example

node_divergence.py, exam from June 2021.

## Node divergence

A graph can be represented using a 2D array where every row contains a triplet of numbers ( $i, j, w_{i j}$ ) representing one graph edge. Here, $i$ is an index of from-node, $j$ is an index of to-node, and $w_{i j}$ is the weight of the edge from $i$ to $j$. For example, consider the graph in the illustration and its representation using $A$.


A = np.array $([2,7,1],[2,1,1],[5,1,2]$, $[5,7,0.5],[7,2,2.5],[7,5,1],[7,8$, 4], $[9,7,1],[8,9,4]])$

The divergence of node $i$ is defined as

$$
d_{i}=\sum_{\substack{j \\ \text { edgeij }}} w_{i j}-\sum_{\substack{j \\ \text { edgeji }}} w_{j i} .
$$

So $d_{i}$ is the difference between the sum of weights of all edges originating from $i$ and the sum of weights of all edges ending in $i$. For example

$$
d_{7}=(2.5+1+4)-(1+0.5+1)=5
$$

## Problem definition

Create a function node_divergence that takes a 2D array representing a graph as input. The function should return an array containing sorted indices for graph nodes in one column and the divergence values for the corresponding nodes in the second column.

## Node Divergence Solution

```
import numpy as np
def node_divergence(A):
    nodes = np.unique(A[:, :2])
    return_arr = np.zeros((nodes.shape[0], 2))
    return_arr[:, 0] = nodes
    for i in range(nodes.shape[0]):
        node = nodes[i]
        divergence = A[A[:, 0] == node, 2].sum() - A[A[:, 1] == node, 2].sum()
        return_arr[i, 1] = divergence
    return return_arr
```

